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USL Technical Memorandum No.

RERADIATED WAVEFORM FOR AN ELLIPTICALLY SYMMETRIC

RERADIATION FUNCTION IN THE FORM OF A LAGUERRE POLYNOMIAL

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(USL PROGRAM NO. 0838)

TRANSFER FUNCTION, IMPULSE RESPONSE AND

20 March 1967

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TRANSFER FUNCTION, IMPULSE RESPONSE AND RERADIATED WAVEFORM FOR AN ELLIPTICALLY SYMMETRIC REPADIATION FUNCTION IN THE FORM OF A LAGUERRE POLYNOMIAL (USL PROGRAM NO. 0838)

by

Donald A. Stremsky

USL Technical Memorandum No. 2242-111-67

20 March 1967

INTRODUCTION

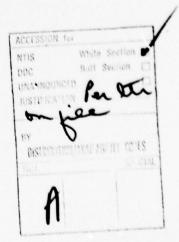
A computational program has been prepared by the Information Processing Division to compute a particular Reradiation Function w(x), Transfer Function W(w,P), Impulse Response w(t,P), and Reradiated Waveform g(t,P) as defined below in terms of the incident plane wave pulse. This IBM 704 Program designated USL Program No. 0838, is in Fortran II language and is described in Appendixes A and B. Similar computational programs are described in USL Technical Memorahdum No. 2242-156-67 and 2242-157-67.

THEORY

Reference (a) contains a description of the mathematical model constructed and the theory behind considering reflection as a reradiation phenomenon.

This program computes for integer values of 3

- $(a) \ a_1 \ a_2 \ w \ (x)$
- (b) W (w,P)



where

$$(1) \quad w(\mathbf{x}) = \frac{(-1)^n 2 \pi}{a_1 a_2}$$

$$(2) \quad w(\mathbf{w}, \mathbf{P}) = e^{-\frac{1}{2}(\mathbf{k} \mathbf{w})^2} \int_{-\infty}^{\infty} \left[(\mathbf{k} \mathbf{w})^2 \right]$$

$$\mathbf{k} = \frac{1}{2} \left[(a_1 p_1)^2 + (a_2 p_2)^2 \right]^{1/2}$$

$$L_n(\mathbf{x}) = \frac{e^n}{n!} \frac{d^n}{d\mathbf{x}^n} \left(e^{-n} \mathbf{x}^n \right)$$

$$= \text{Laguerre polynomial}$$

$$(3) \quad w(\mathbf{t}, \mathbf{P}) = \frac{1}{n!} \frac{e^{-\frac{1}{2}(\mathbf{t}/\mathbf{k})^2}}{e^{-\frac{1}{2}(\mathbf{t}/\mathbf{k})^2}} \left\{ \frac{1}{2} \left(e^{-\frac{1}{2}(\mathbf{x}^2)} \right) \right\}^2$$

$$= \text{Hermite polynomial}$$

$$(4) \quad g(\mathbf{t}, \mathbf{P}) = \int_{-\infty}^{\infty} f(\mathbf{t}) w \left(\mathbf{t} \cdot \mathbf{t}, \mathbf{P} \right) d\mathbf{t}$$

$$f(\mathbf{t}) = \begin{cases} A(\mathbf{t}) \cos ((\omega_0 + \frac{\Delta \mathbf{w}}{2}(\mathbf{t}/\mathbf{t})) + d \\ A(\mathbf{t}) = 0 \end{cases} f(\mathbf{t}) = \mathbf{t}$$

COMPUTER PROGRAM DESCRIPTION

A nomenclature listing for USL Program No. 0838 is Appendix A, the flow chart is Appendix B, and the IBM 704 Fortran II Program is Appendix C.

The basic input data deck required by the program consists of four cards.

Table 1

Card No.	Cols.	Contents
1	1-8	a ₁
	9-16	a 1 a 2
	17-24	x ₁
	25-32	x ₂
	33-40	c
	41-48	c v d
	49-51.)
	52-54	ISKP (set equal to zero to compute
		Reradiation Function)
	55-57	JSKP (set to zero to compute Transfer Function)
	58-60	KSKP (set equal to zero to compute Impulse Response & Reradiated Waveform For long jobs requiring the use of a
		dump tape at least one of the above
		option variables should not be set
		equal to zero.
2	1-8	Initial value of w
	9-16	Maximum value for
	17-24	Initial value of t
	25-32	Initial value of k
	35-36	KK (if set equal to zero, initial
		value of k will be computed)
	39-46	Maximum value of k
3	1-8	λ, Components of λ
	9-16	λ ξ Components of γ
	17-24	λ ₂) N.) Components of N
	25-32	
	33-40	N ₁) Δ × ₁
	41-48	∆ x₂
	49-56	Δ t
	57-64	Increment of w
	65-72	A k

Table 1 (cont'd)

Card No.	Cols.	Contents
4	1-3	Number of values of Reradiation
		Function to compute
	4-11	۸۲
	12-19	Maximum value for t
	20-27	wo
	28-35	Δ W
	36-43	Maximum value of 7
	44-51	Initial value of 7
	52-59	0

FORMATS

Card No. 1 - Format 6F8.3, 4I3

2 - Format 4F8.3,2x,I2,2x,F8.3

3 - Format 9F8.3

4 - Format 13, 7F8.3

Tape Units Required

Tape Unit No.	Tape Identification
3	Data input
4	Values for Reradiation Function, Transfer Function, and Impulse
5	Response Calcomp Plotter containing
,	values for Reradiation Function
6 7	Reradiated waveform array (k,t) Transfer Function Array (k,w)

Tape Units Required (cont'd)

Tape Unit No.

Tape Identification

8

Impulse Response Array (k,t)

SS-5 must be down to dump No other sense switches are used

Dump Tape

Subroutine Amp required - computes values of A array referred to under equation 4.

PROGRAM OUTPUT

Tape #4 contains:

- (1) The values for the ? array plus the corresponding values for the Reradiation Function according to Format (1x, F10.5, 5x, F10.5)
- (2) The values for the product of k and w plus the corresponding values of the Transfer Function according to Format (1x, F10.5, 5x, F10.5)
- (3) The values for t/k plus the corresponding values for the Impulse Response according to Format (1x, F10.5, 5x, F10.5)

Tape #5 contains:

The values for the Reradiation Function (Calcomp Plotter tape)

Tape #6 contains:

The Reradiated Waveform Array (k,t) according to Format (F10.5)

Tape #7 contains:

The Transfer Function Array (k,w) with Format (F10.5)

Tape #8 contains:

The Impulse Response Array according to Format (F10.5)

Tape #0 is a dump tape.

Notes: This program contains options to compute or not to compute any of the functions mentioned above. Tapes Unit Nos. 6, 7, and 8 can be used as input to USL Program No. 0809, "Representation of Surfaces: A Computer Program to Plot Contours and Draw Perspective Views", by Edward Beardsworth, Jr.

SUMMARY

An IBM 704 Fortran program, USL Program No. 0838, has been written to compute a particular Reradiation Function, Transfer Function, Impulse Response, and Reradiated Waveform in terms of the incident plane wave pulse.

D. A. STREMSKY Mathematician

LIST OF REFERENCES

(a) Edward S. Eby, "Spectra and Waveforms of Bottom Reflected Pulses", USL Tech. Memo. No. 914-160-66 of 10 June 1966.

APPENDIX A

NOMENCLATURE LISTING FOR USL PROGRAM NO. 0838

S(I)	$\left(\frac{x_{i}}{q_{i}}\right)^{2} + \left(\frac{x_{i}}{q_{i}}\right)^{2}$
Z(1)	VS(I)
RERAD (I)	Element of Reradiation Function Array
TRFER (I)	Element of Transfer Function Array
AKW (LM,I)	k.w
RESP (LM,I)	Element of Impulse Response Array
RATIO (IM,I)	t/k
GSUM (LM,J)	Element of Reradiated Waveform Array
A 1	a ₁
A2	e ₂
XI.	x ₁
X2	x ₂
c	c
V	v
N	>
W	W
WMAX	Maximum value for w
T	Initial value for t
AK	k
AKMAX	Maximum value for k

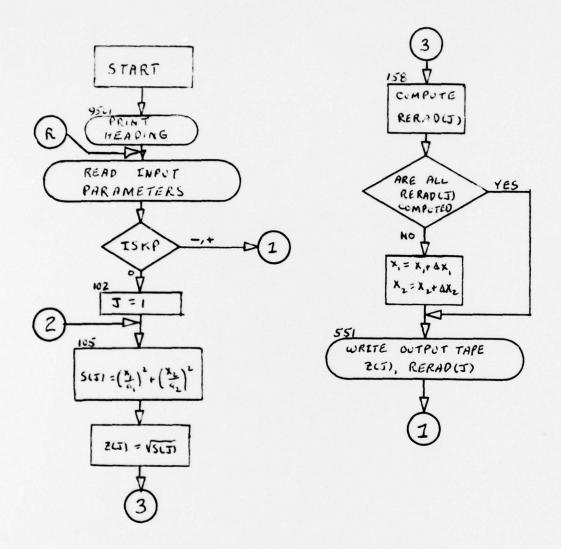
B1	λ, 2
B2	λ_2 components of λ
33	N, 2
B ¹ +	N ₂ components of N
35	Δ ^x l
36	Δ ×2
В7	Δt
В8	Increment of w
310	Δ Υ
B12	∆ k
Omega	ω_{\bullet}
DELTA	A W
TT	Maximum value for 7
TAV	Initial value of γ
PHI	d
ND.	Number of values of Reradiation Function to compute
TMAX	Maximum value for T

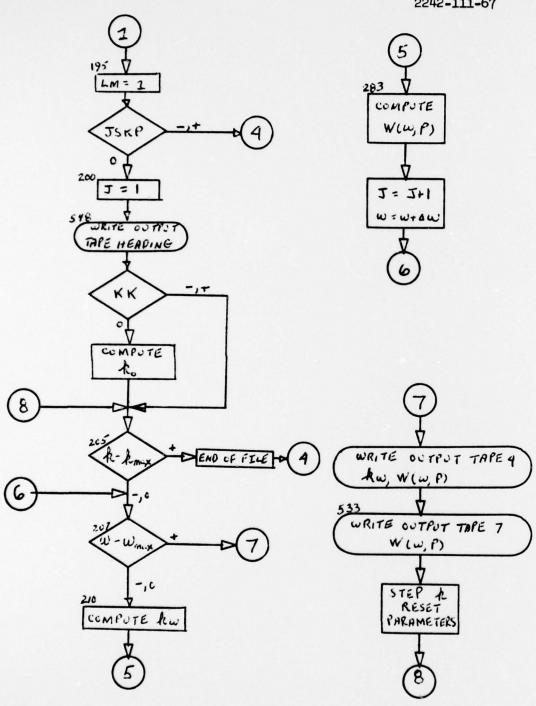
APPENDIX B

FLOW CHART FOR USL PROGRAM NO. 0838

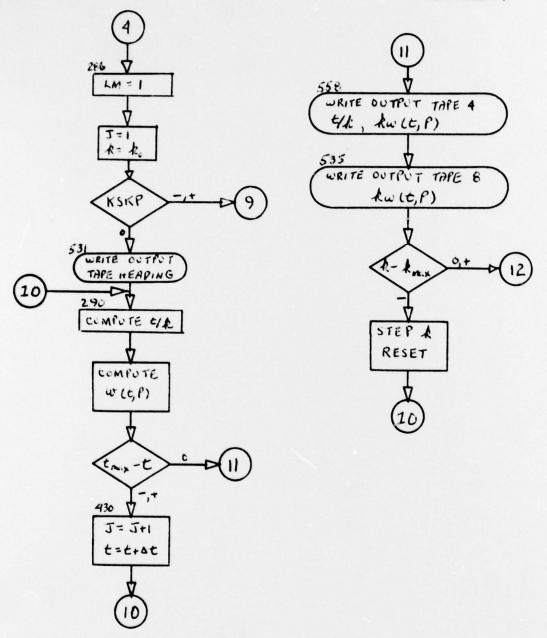
"RERADIATION FUNCTION, TRANSFER FUNCTION, IMPULSE RESPONSE (CASE 2)"

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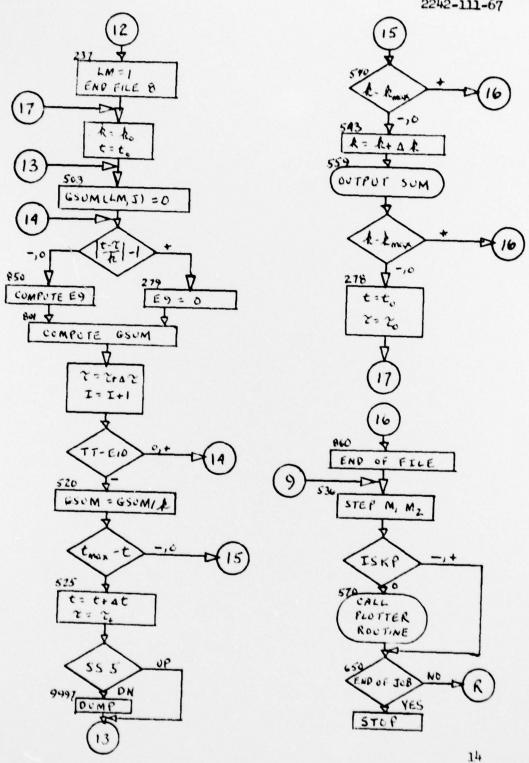




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APPENDIX C
FORTRAN PROGRAM NO. 0838

```
RERADIATION FUNCTION-TRANSFER FUNCTION-IMPULSE RESPONSE (CASE 2)
C
      D.A. STREMSKY
      DIMENSION Z (500) . RERAD (500) . TRF ER (50.50) . AKW (50.50) . RAT [0 (50.50) . R
     1ESP(50.50).SUM(50).HSUM(50).S(500).GSUM(50.50).R(1000).IDUMP(18)
      DIMENSION BUFFER (1024) .XAXIS (500) .YAXIS (500)
STOJN ALF
             *0838
STECO ALF
      WRITE CUTPUT TAPE 4.9501
 9501 FCRMAT(1H1)
      READ INPUT TAPE 3.9502.DI
 9502 FCRMAT (A5)
      IF (TDJN-DI) 9503 . 9504 . 9503
 9503 PAUSE 6
 9504 WRITE CUTPUT TAPE 4.9502.DI
      WRITE CUTPUT TAPE 4.9505
 9505 FCRMAT(10X32HD.A.STREMSKY.ROOM 3126.CODE 2242)
      READ INPUT TAPE 3.100.A1.A2.X1.X2.C.V.N.ISKP.JSKP.KSKP
  100 FCRMAT (6F8.3.413)
      READ INPUT TAPE 3.101.W.WMAX.T.AK.KK.AKMAX
  101 FCRMAT (4F8.3.2X.12.2X.F8.3)
      READ INPUT TAPE 3.103.81.82.83.84.85.86.87.88.812
  103 FCRMAT (9F8.3)
READ INPUT TAPE 3.104.N1.B10.TMAX.AMEGA.DELTA.TT.TAU.PHI
  104 FORMAT (13.7F8.3)
      41=h
      AK 1 = AK
      TIET
      TAU1=TAU
      PIE=3.1415
      PCP=2.5066
      DEG=180./PIE
      NP1=N+1
      NP2=N+2
      SUM (1) = 0.
      SUM (2)=1.
      IF (ISKP) 195 . 102 . 195
  102 J=1
105 S(J)=(X1/A1)**7+(X2/A2)**2
      Zx=5(.1)
      Z(J)=SCRTF(ZX)
      IF (N) 156 . 156 . 157
  156 SIGN=1.
      GC TC 158
  157 SIGN= (-1) **N
  158 RERAD(J)=SIGN#2.C#PIE#A1#A2
      IF (N1-J) 546 . 546 . 175
  175 J=J+1
      X1=X1+P5
      X2=X2+P6
      GC TC 105
  546 WRITE OUTPUT TAPE 4.551
  551 FCRMAT(1X36HZ
                                     REPADIATION FUNCTION)
      WRITE OUTPUT TAPE 4.552.(Z(I) .RERAD(I) .I=1.N1)
  552 FCRMAT(1X+F10+5+5X+F10+5)
      WRITE CUTPUT TAPE 4.553
  553 FCRMAT (///)
  195 LN=1
```

```
IF (J5KP) 286 . 200 . 266
200 J=1
548 WRITE CUTPUT TAPE 4.554
554 FCRNAT (1X34HKW
                                     TRANSFER FUNCTION)
    IF (KK) 205 + 202 + 205
202 P1=81-C*83/V
    P2=B2-C*84/V
    CP= (A1*P1) **2+ (A2*P2) **2
    AK=SGRTF (CB) /C
205 IF (AK-AKMAX) 207.207.285
207 IF (W-WMAX) 210 . 210 . 250
210 AKW (LM.J) = AK +W
    RZ=AKW(LM.J) **2
    R3=-R2/2.
    CCEF1=EXPF(R3)
    IF(N)230.230.215
215 CC 225 I=3.NP2
    A1M3=1-3
    IM1=1-1
    IM2=1-2
    PAR=2. +AIM3+1.-R2
    PART=AIM3**2
    SUM(I) =-PAR*SUM(IM1) -PART*SUM(IM2)
225 CONTINUE
230 NPROD=1
    IF(N)280+280+260
260 DC 275 L=1.N
    NEWL=L
    NPRCD=NPRCD*NEWL
275 CONTINUE
280 PRCD=NPROD
    IF (N) 281 • 281 • 282
281 SIGN=1.
    GC TC 283
282 SIGN= (-1) **N
283 TRFER(LM+J)=CCEF1+SUM(NP2)+SIGN/PROD
    J=J+1
    W=W+B8
    GC TC 207
250 N2=J-1
    N4ELM
    WRITE CUTPUT TAPE 4.555. ((AKW(LM.I).TRFER(LM.I).I=1.N2).LM=N4.N4)
555 FORMAT (1X .F10 .5 .5X .F10 .5)
533 WRITE OUTPUT TAPE 7.515.((TRFER(LM.I).I=1.N2).LM=N4.N4)
515 FCRMAT (F10.5)
    J=1
    WEW1
    LN=LN+1
    AK=AK+B12
GC TC 205
285 END FILE 7
    END FILE 7
286 LN=1
    J=1
    AK = AK 1
IF (KSKP) 536 . 531 . 536
531 WRITE CUTPUT TAPE 4.557
557 FCRMAT (1X34HT/K
                                      IMPULSE RESPONSE)
```

```
290 RATIC (LM.J) =T/AK
    GZ=RATIO(LM.J) **2
    63=-62/2.
    IF (J5KP) 291 . 297 . 291
291 NPRCD=1.
    IF (N) 296 . 296 . 292
292 DC 295 L=1.N
    NEWL=L
    NPRCD=NPRCD+NEWL
295 CONTINUE
296 PRCD=APROD
297 DEN=PROD*POP
    G4=EXPF (G3)
    CCEF2=G4/DEN
    G5=RATIC(LM.J)
    IF (G5) 300 • 320 • 320
300 66=-65
    GC TC 350
320 G6=G5
350 HSUM (1) =0.
    HSUM (2)=1.
    IF (N) 410 • 410 • 360
360 DC 400 K=3.NP2
    AKM3=K-3
    KM1=K-1
    KM2=K-2
    HSUM (K) =G6*HSUM (KM1) -AKM3*HSUM (KM2)
400 CONTINUE
410 G7=HSUM (NP2)
    G8=G7++2
425 RESP(LM.J) = COEF2*GR
    IF (TMAX-T) 500 +430 +430
430 J=J+1
    T=T+87
    GC TC 290
500 N3=J-1
    N4=LM
    WRITE CUTPUT TAPE 4.558.((RATIO(LM.I).RESP(LM.I).I=1.N3).LM=N4.N4)
558 FCRMAT(1X+F10.5+5X+F10.5)
535 WRITE CUTPUT TAPE 8.516. ((RESP(LM.1). 1=1.N3) . LM=N4.N4)
516 FCRMAT (F10.5)
    IF (AK-AKMAX) 495 . 237 . 237
495 AK=AK+F12
    LN=LM+1
    J=1
    T=T1
    GC TC 290
237 LM=1
    END FILE 8
    END FILE 8
    N5=0
    AK = AK 1
    1=1
502 C11=R7/AK
    TETI
    J=1
    C12=ARSF (D11)
503 GSUN ([N.J) =0.
```

```
505 FRACT=TAU/TT
          F1=AMEGA+DELTA*FRACT/2.0
     E2=F1+TAU
     E3=E2+PHI
     E4=CCSF (E3/DEG)
     CALL AMP (TAU . R)
     FCN=R(1) *E4
     TOIF= (T-TAU) /AK
     GRAPE=ABSF (TDIF)
     PLUM=GRAPE-1.0
     IF (PLUM) 850 . 850 . 279
 279 E9=0.0
     GC TC 801
 850 E5=GRAPE/D12
     NES=ES
     IA=NE5+1
     IB=NE5+2
     E6=GRAPE-RATIC (LM.IA)
     E7=E6/D11
     E8=1.0-E7
     RSPN=E7*RESP(LM.IB)+E8*RESP(LM.IA)
     E9=FCN*RSPN*B10
 801 GSUM(LM.J)=GSUM(LM.J)+E9
     TAU=TAU+810
     I=I+1
     E10=ARSF (TAU)
     IF (TT-E10) 520 . 505 . 505
 520 GSUM (IM . J) = GSUM (LM . J) /AK
     IF (TMAX-T) 540 + 540 + 525
 525 T=T+87
     J=J+1
     TAU=TAU1
     IF (SENSE SWITCH 5) 9997.9999
9997 CC 9998 LK=1+15
     IDUMP (LK) =+0
9998 CONTINUE
     IDLMP (16) =-6
     ICUMP (17) =+0
     ICUMP (18) = N5
     CALL DUMP (IDUMP)
9999 GC TC 503
540 IF (AK-AKMAX) 543.543.860
 543 AK = AK + P12
     N3=J-1
     N4=LM
     WRITE OUTPUT TAPE 6.559. ((GSUM(LM.I).I=1.N3).LM=N4.N4)
 559 FORMAT (F10.5)
     N5=N5+J
     IF (AK-AKMAX) 278 . 278 . 860
 278 LM=LM+1
     T=T1
     TAU=TAU1
     1=1
     CC TC 502
 860 END FILE 6
     END FILE 6
 536 MI=N1+1
     M2=N1+2
```

```
IF (15KP) 650.570.650
 570 CALL PLOTS (BUFFER (1024) . 1024 . 5)
      DC 560 J=1.N1
      XAXIS(J)=Z(J)
      YAXIS(J) = RERAD(J)
 560 CONTINUE
      CALL PLOT (0.0.5.0.-3)
      CALL SCALE (YAXIS.5.0.N1.1.10.0)
      CALL SCALE (XAXIS.10.0.N1.1.10.0)
      CALL LINE (XAXIS.YAXIS.NI.1.1.1)
CALL AXIS (0.0.0.0.20HRERADIATION FUNCTION.20.5.0.90.0.YAXIS(M1).Y
     1AXIS(M2) .10.0)
CALL AXIS (0.0.0.0.1HZ.-1.10.0.0.0.XAXIS(M1).XAXIS(M2).10.0)
CALL PLOT (0.0.0.0.999)
650 READ INPUT TAPE 3.9502.ED
      IF (ED-TEOD) 9503 . 9509 . 9503
9509 WRITE CUTPUT TAPE 4.9511
9511 FORMAT (4HOEND)
      END FILE 4
9510 STOP 5
      END (1 . 1 . 0 . 1 . 1)
```